## Paper 1: NUMERICAL ANALYSIS - 2014

Note: Attempt any two parts from each question. All questions carry equal marks. Simple/scientific calculator is allowed.

## UNIT - 1

- 1. (a) Find the root of the equation :  $x^3 x 4 = 0$  using the bisection method.
  - (b) Find the root of  $x^2 5x + 2 = 0$  correct of five decimal places by Newton-Raphson method.
  - (c) Solve the equation :  $6 x^4 13 x^3 35 x^2 x + 3 = 0$  one root being  $2 \sqrt{3}$ .

2. (a) Solve the equations:

$$x + 4y - z = -5$$
  
 $x + y - 6z = -12$ 

$$3x - y - z = 4$$

Using Gauss-Jordan method.

(b) Solve the system of linear equations:

$$x + 2y + 3z = 5$$
  
 $2x + 8y + 22z = 6$   
 $3x + 22y + 82z = -10$ 

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Using the Cholesky method.

(c) Find the inverse of the matrix:

$$A = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix}$$

by Gauss-Jordan method.

## UNIT - 3

3. (a) Interpolate f (2) from the following data:

and explain why the value obtained is different from that obtained by putting x = 2 in the expression  $2^x + 5$ .

- (b) Compute f(2, 4, 9, 10) when :  $f(x) = x^4 + x^2 + 1$
- (c) Find the value of x correct to two decimal places lying between 15 and 20 satisfying the equation :

$$x^2 + 250 \log_{10} x = 635$$

## **UNIT - 4**

Given :

$$x$$
 0.1 0.2 0.3 0.4  
 $y = f(x)$  1.10517 1.22140 1.34986 1.49182  
Find  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$  at  $x = 0.4$ 

(b) Show that:

$$\int_0^1 \frac{dx}{1+x} = 0.69315$$

(c) Using Simpson's '1/3' rule evaluate:

$$\int_{0.5}^{0.7} x^{1/2} e^{-x} dx$$
UNIT - 5

5. (a) Use Picard's method to approximate y when x = 0.1, x = 0.2, given that :

$$y = 0$$
,  $x = 0$ ,  $\frac{dy}{dx} = x + y$ 

(b) Solve  $\frac{dy}{dx} = 1 - 2xy$  given that y (0) = 0 by Taylor's series.

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(c) Use Runge-Kutta method of fourth order to solve: y' = xy for x = 1.2. Initially x = 1, y = 2 (take h = 0.1).

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